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14. ABSTRACT The goals of the project are to discover new quantum algorithms; develop novel paradigms for constructing quantum algorithms; develop complexity-theoretic results that relate to quantum algorithms; and develop theoretical approaches for the implementation of quantum algorithms.  Building on the pioneering work of Shor and Grover, the field of quantum algorithms has developed substantially, providing several insights about the underlying mechanisms behind quantum algorithms, as well as their limitations. Moreover, recent					
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## Report Title

QCCM Center for Quantum Algorithms

### ABSTRACT

The goals of the project are to discover new quantum algorithms; develop novel paradigms for constructing quantum algorithms; develop complexity-theoretic results that relate to quantum algorithms; and develop theoretical approaches for the implementation of quantum algorithms.

Building on the pioneering work of Shor and Grover, the field of quantum algorithms has developed substantially, providing several insights about the underlying mechanisms behind quantum algorithms, as well as their limitations. Moreover, recent work on novel paradigms for designing quantum algorithms (e.g., quantum walks and adiabatic computing), as well as theoretical advances relating algorithms to physical implementations (e.g., efficient error-correction techniques) point to promising directions for future development. Our focus is on searching for new algorithms and investigating the limitations of quantum information processing. Moreover, this is complemented by an investigation of quantum error-correction, the accuracy threshold for a variety of error models, focused on reducing overhead for implementations.

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**List of papers submitted or published that acknowledge ARO support during this reporting period. List the papers, including journal references, in the following categories:**

**(a) Papers published in peer-reviewed journals (N/A for none)**

## 2006 Publications:

A nearly optimal discrete query quantum algorithm for evaluating NAND formulas

A. Ambainis 0704.3628v1

A New Quantum Lower Bound Method with Applications to Direct Product Theorems and Time-Space Tradeoffs

A. Ambainis, R. Spalek, R. de Wolf. quant-ph/0511200

Algebraic results on quantum automata

A. Ambainis, M. Beaudry, M. Golovkins, A. Kikusts, M. Mercer, D. Thrien

Theory of Computing Systems 39(2006), pages 165-188

Benchmarking Quantum Control Methods on a 12-Qubit System

C. Negrevergne, T.S. Mahesh, C.A. Ryan, M.J. Ditty, F. Cyr-Racine, W. Power, N. Boulant, T. Havel, D.G. Cory, R. Laflamme

Phys. Rev. Lett. 96, 170501 (2006)

Classical Interaction Cannot Replace a Quantum Message

D. Gavinsky quant-ph/0703215v2

Communicating over adversarial quantum channels using quantum list codes

Debbie Leung, Graeme Smith

IEEE Trans. Info. Theory 54, 2, 883-887 (2008) quant-ph/0605086

Discrete-query quantum algorithm for NAND trees

A. M. Childs and R. Cleve and S. P. Jordan and D. Yeung quant-ph/0702160v1

Exact and Approximate Unitary 2-Designs: Constructions and Applications

C. Dankert and R. Cleve and J. Emerson and E. Livine quant-ph/0606161v1

Exponential Separation of Quantum and Classical One-Way Communication Complexity for a Boolean Function

D. Gavinsky and J. Kempe and R. de Wolf quant-ph/0607174v1

Finding flows in the one-way measurement model

Niel de Beaudrap arXiv:quant-ph/0611284

Interaction in Quantum Communication

Hartmut Klauck, Ashwin Nayak, Amnon Ta-Shma, and David Zuckerman

quant-ph/0603135

Models of Quantum Cellular Automata

C. A. Perez-Delgado and D. Cheung

quant-ph/0508164v1

New Limits on Fault-Tolerant Quantum Computation

H. Buhrman and R. Cleve and M. Laurent and N. Linden and A. Schrijver and F. Unger

quant-ph/0604141v2

On the Role of Shared Entanglement

D. Gavinsky

quant-ph/0604052v2

Operator quantum error correction

D. W. Kribs and R. Laflamme and D. Poulin and M. Lesosky

Quant. Inf. & Comp., 6, 383 (2006)

quant-ph/0504189v3

Optimal quantum circuits for general phase estimation

W. van Dam and G. M. D'Ariano and A. Ekert and C. Macchiavello and M. Mosca  
quant-ph/0609160v1

Phase map decompositions for unitaries

Niel de Beaudrap, Vincent Danos, Elham Kashefi  
quant-ph/0603266

Polynomial degree vs. quantum query complexity

A. Ambainis  
Journal of Computer and System Sciences, 72 (2006), pages 220-238

Quantum Algorithms and Complexity

M. Mosca  
Proceedings of NATO ASI Quantum Computation and Information 2005, Chania, Crete, Greece, IOS Press (2006), in press

Quantum Cellular Automata and Single Spin Measurement

C. Perez, D. Cheung, M. Mosca, P. Cappellaro, D. Cory  
Proceedings of Asian Conference on Quantum Information Science, Beijing, China

Quantum Circuit Simplification and Level Compaction

D. Maslov and G. W. Dueck and D. M. Miller  
quant-ph/0604001v1

Quantum Complexity of Testing Group Commutativity

Frederic Magniez and Ashwin Nayak  
quant-ph/0506265

Quantum Error Correcting Codes From The Compression Formalism

M. Choi and D. W. Kribs and K. Zyczkowski  
Rep. Math. Phys., 58, 77 (2006) Quant-ph/0511101v2  
Quantum Error Correcting Subsystems are Unitarily Recoverable Subsystems  
D. W. Kribs and R. W. Spekkens  
Phys. Rev. A 74, 042329 (2006)  
quant-ph/0608045v2

Quantum search with variable times

A. Ambainis  
quant-ph/0609168v1

Quantum Versus Classical Proofs and Advice

S. Aaronson and G. Kuperberg  
quant-ph/0604056v3

Quantum Walk on a Line with Two Entangled Particles

Y. Omar, N. Paunkovic, L. Sheridan, S. Bose  
Phys. Rev. A 74, 042304 (2006) quant-ph/0411065

Search via Quantum Walk

F. Magniez and A. Nayak and J. Roland and M. Santha  
quant-ph/0608026v3

Self-Testing of Quantum Circuits

Frederic Magniez, Dominic Mayers, Michele Mosca, Harold Ollivier  
Proceedings of the 33rd International Colloquium on Automata, Languages and Programming (ICALP'06), Venice, Italy

Simple proof of fault tolerance in the graph-state model

P. Aliferis and D. W. Leung

Phys. Rev. A 73, 032308 (2006)

quant-ph/0503130v4

Strengths and Weaknesses of Quantum Fingerprinting

D. Gavinsky and J. Kempe and R. de Wolf

quant-ph/0603173v1

Strong Parallel Repetition Theorem for Quantum XOR Proof Systems

R. Cleve and W. Slofstra and F. Unger and S. Upadhyay

quant-ph/0608146v1

The Learnability of Quantum States

S. Aaronson

quant-ph/0608142v3

Toward a general theory of quantum games

G. Gutoski and J. Watrous

quant-ph/0611234v2

Two-way entanglement purification for finite block size

A. Ambainis, D. Gottesman.

IEEE Transactions on Information Theory, 52 (2006)

The minimum distance problem for two-way entanglement purification.

Andris Ambainis, Daniel Gottesman

IEEE Transactions on Information Theory, 52(2): 748-753 (2006)

Quantum algorithms for matching and network flows

A. Ambainis, R. Spalek.

Proceedings of STACS'06, Lecture Notes in Computer Science, 3884 (2006), pages 172-183. quant-ph/0508205

Quantum computing with highly mixed states.

Andris Ambainis, Leonard Schulman, Umesh Vazirani.

Journal of the ACM, 53:507-531 (2006).

Quantum direct product theorems for symmetric functions and time-space tradeoffs

A. Ambainis, R. Spalek, R. de Wolf.

quant-ph/0511200, combined version of this and the previous paper has been accepted to STOC'06.

QMA/qpoly is contained in PSPACE/poly: de-Merlinizing quantum protocols

S. Aaronson

Proceedings of IEEE Complexity 2006. quant-ph/0510230.

Oracles are subtle but not malicious

S. Aaronson

Proceedings of IEEE Complexity 2006. cs.CC/0504048.

Classical and quantum fingerprinting with shared randomness and one-sided error

R.T. Horn, A.J. Scott, J. Walgate, R. Cleve, A.I. Lvovsky, and B.C. Sanders

Quantum Information and Computation, 5(3), 258--271 (2005).

Quantum lower bounds for the Goldreich-Levin problem

M. Adcock, R. Cleve, K. Iwama, R. Putra, and S. Yamashita

Information Processing Letters, 97(5), 208--211 (2005).

Efficient quantum algorithms for simulating sparse Hamiltonians

D.W. Berry, G. Ahokas, R. Cleve, and B.C. Sanders

Accepted with minor revisions for publication in Communications in Mathematical Physics on 23 May 2006.

Additivity of quantum two-prover interactive proof systems

R. Cleve, W. Slofstra, F. Unger, and S. Upadhyay.

Submitted 2006.

A unified and generalized approach to quantum error correction

D. Kribs, R. Laflamme, and D. Poulin.

Phys. Rev. Lett.

Pauli measurement are universal

V. Danos and E. Kashefi

Proceedings of the 3rd Workshop on Quantum Programming Languages, QPLO5 (2005).

Distributed measurement-based quantum computing

V. Danos, E. D'Hondt, E. Kashefi and P. Panangaden

Proceedings of the 3rd Workshop on Quantum Programming Languages, QPLO5 (2005).

Noiseless subsystems for collective rotation channels in quantum information theory

J.A. Holbrook, D. Kribs, R. Laflamme and D. Poulin

Integral Equations & Operator Theory, 51 (2) 215-234 (2005).

Lower Bounds on the Deterministic and Quantum Communication Complexities of Hamming-Distance Problems.

Andris Ambainis, William I. Gasarch, Aravind Srinivasan, Andrey Utis

Proceedings of ISAAC 2006, pp. 628-637

Improved Algorithms for Quantum Identification of Boolean Oracles.

Andris Ambainis, Kazuo Iwama, Akinori Kawachi, Rudy Raymond Harry Putra, Shigeru Yamashita

Proceedings of SWAT 2006, pp. 280-291

Quantum Identification of Boolean Oracles. A chapter in H. Imai, M. Hayashi (eds.)

Andris Ambainis, Kazuo Iwama, Akinori Kawachi, Rudy Raymond Harry Putra, Shigeru Yamashita

Quantum Computation and Information: From Theory to Experiment, Topics in Applied Physics, vol. 102, pp. 1-18 (2006)

Quantum walk algorithm for element distinctness.

Andris Ambainis

SIAM Journal on Computing, accepted for publication.

Approximate randomization of quantum states with fewer bits of key.

P. A. Dickinson and A. Nayak.

In Quantum Computing Back Action 2006, volume 864 of AIP Conference Proceedings, pages 18–36. Springer, New York, 2006. Refereed Volume.

Limits on the ability of quantum states to convey classical messages.

A. Nayak and J. Salzman.

Journal of the ACM, 53(1):184–206, Jan. 2006.

Invertible quantum operations and perfect encryption of quantum states.

A. Nayak and P. Sen.

Quantum Information and Computation, Jul. 2006. 7 pages.

Accessible versus holevo information for a binary random variable.

R. Jain and A. Nayak.

Technical Report quant-ph/0603278, ArXiv.org Preprint Archive, Mar. 2006. Submitted to Quantum Information and Computation. 7 pages.

Quantum key distribution based on arbitrarily-weak distillable entangled states  
Karol Horodecki, Debbie W. Leung, Hoi-Kwong Lo, Jonathan Oppenheim  
5 pages, double column (with page limit of 4) Journal Reference: Phys. Rev. Lett, 96 (2006) 070501.

Two-way quantum communication channels  
Andrew M. Childs, Debbie W. Leung, Hoi-Kwong Lo  
21 pages, single column  
International Journal of Quantum Information, Memorial issue for Asher Peres 4 (2006) 63-83.

Fault-tolerant quantum computation in the graph-state model  
Panos Aliferis, Debbie W. Leung  
6 pages, double column (shortest derivation of that particular threshold theorem to-date)  
Phys. Rev. A, 73 (2006) 032308.

Aspects of generic entanglement  
Patrick M. Hayden, Debbie W. Leung, Andreas Winter  
22 pages, single column  
Comm. Math. Phys. 265 (2006) 95-117.

Typical entanglement of stabilizer states  
G. Smith and D. Leung  
10 pages, double column, quant-ph/0510232, in print for Phys. Rev. A.

Zero-knowledge against quantum attacks.  
J. Watrous  
Proceedings of the 38th ACM Symposium on Theory of Computing (STOC), pages 296–305, 2006.

Single spin measurement using cellular automata techniques  
C. Perez, M. Mosca, P. Cappelaro, D. Cory  
Physical Review Letters, (2006).

Witnessing effective entanglement in a continuous variable prepare & measure setup and application to a QKD scheme using postselection  
S. Lorenz, J. Rigas, M. Heid, U.L. Andersen, N. Lütkenhaus, G. Leuchs  
Phys. Rev. A 74, 042326 (2006) (9 pages)

Upper bound on the secret key rate distillable from effective quantum correlations with imperfect detectors  
T. Moroder, M. Curty, N. Lütkenhaus  
PRA 73, 012311 (2006) (9 pages)

Entanglement verification for quantum-key-distribution systems with an underlying bipartite qubit-mode structure  
J. Rigas, O. Gühne, N. Lütkenhaus  
PRA 73, 012341 (2006) (6 pages)

Efficiency of coherent-state quantum cryptography in the presence of loss: Influence of realistic error correction  
M. Heid and N. Lütkenhaus  
PRA A 73, 052316 (2006) (7 pages)

Implementing Non-Projective Measurements via Linear Optics: an Approach Based on Optimal Quantum State Discrimination  
P. van Loock, K. Nemoto, W. J. Munro, P. Raynal, N. Lütkenhaus  
PRA 73, 062320 (2006) (13 pages)

2007 Publications:

Quantum network communication – the butterfly and beyond

D. Leung, J. Oppenheim and A. Winter

13 pages, double column, quant-ph/0608223 accepted for presentation in QIP 2007

An extremal result for geometries in the one-way measurement model

Niel de Beaudrap, Martin Pei

To appear in QIC

arXiv:quant-ph/0702229

Direct Product Theorems for Communication Complexity via Subdistribution Bounds

Rahul Jain, Hartmut Klauck, and Ashwin Nayak

ECCC Technical Report TR07-064

Distinguishing Short Quantum Computations

Bill Rosgen

STACS 2008

arXiv:0712.2595v1

Efficient quantum algorithms for simulating sparse Hamiltonians

D. W. Berry and G. Ahokas and R. Cleve and B. C. Sanders

Comm. Math. Phys. 270, 359 (2007)

quant-ph/0508139v2

Entanglement-Resistant Two-Prover Interactive Proof Systems and Non-Adaptive Private Information Retrieval Systems

R. Cleve and D. Gavinsky and R. Jain

0707.1729v1

Experimentally scalable protocol for identification of correctable codes

Marcus Silva, Easwar Magesan, David W. Kribs, Joseph Emerson

arXiv:0710.1900

Exponential Separation of Quantum and Classical Non-Interactive Multi-Party Communication Complexity

D. Gavinsky and P. Pudl'ak

0708.0859v1

General optimized schemes for phase estimation

G. M. D'Ariano, W. van Dam, E. Ekert, C. Macchiavello, and M. Mosca

Physical Review Letters, Volume 98, Number 9, Article 090501

Generalization of Quantum Error Correction via the Heisenberg Picture and Application to Information Flow

Cedric Beny, Achim Kempf, David W. Kribs

Phys. Rev. Lett. 98, 100502 (2007)

quant-ph/0608071

Interaction in Quantum Communication

Hartmut Klauck, Ashwin Nayak, Amnon Ta-Shma, and David Zuckerman

IEEE Transactions on Information Theory, 53(6), pages 1970--1982, June 2007

Limitations of some simple adiabatic quantum algorithms

L. M. Ioannou and M. Mosca

quant-ph/0702241v1

Linear Depth Stabilizer and Quantum Fourier Transformation Circuits with no Auxiliary Qubits in Finite Neighbor Quantum Architectures

D. Maslov

quant-ph/0703211v1



Local Unitary Quantum Cellular Automata  
Carlos A. Pérez-Delgado and Donny Cheung  
Phys. Rev. A 76, 032320 (2007) (15 pages)  
arXiv:0709.0006

Optimal phase estimation in quantum networks  
G. M. D'Ariano, W. van Dam, E. Ekert, C. Macchiavello, and M. Mosca  
Journal of Physics A: Math. Theor. 40, 7971-7984

Quantum Circuit Placement: Optimizing Qubit-to-qubit Interactions through Mapping Quantum Circuits into a Physical Experiment  
D. Maslov, S. M. Falconer, and M. Mosca  
Proceedings of ACM/IEEE Design Automation Conference, pp. 962-966, San Diego, CA, 2007  
quant-ph/0703256

Quantum Complexity of Testing Group Commutativity  
Frederic Magniez and Ashwin Nayak  
Algorithmica, 48(3), pages 221--232, 2007

Quantum t-designs: t-wise independence in the quantum world  
A. Ambainis and J. Emerson  
quant-ph/0701126v2

Search via Quantum Walk  
Frederic Magniez, Ashwin Nayak, Jeremie Roland, and Miklos Santha  
In Proceedings of the Thirty-Ninth Annual ACM Symposium on the Theory of Computing, 575 - 584, 2007

Self-testing of universal and fault-tolerant sets of quantum gates  
W. van Dam, F. Magniez, M. Mosca and M. Santha  
SIAM Journal on Computing, Vol. 37, No. 2  
611-629 (2007)

Perfect Parallel Repetition Theorem for Quantum XOR Proof Systems  
R. Cleve, W. Slofstra, F. Unger and S. Upadhyay  
In Proceedings of the 22nd IEEE Conference on Computational Complexity (CCC), pages 109–114, 2007.

Toward a general theory of quantum games  
G. Gutoski and J. Watrous  
In Proceedings of the 39th ACM Symposium on Theory of Computing (STOC'07), pages 565–574, 2007.

An Introduction to Quantum Computation  
P. Kaye, R. Laflamme, M. Mosca  
Oxford University Press, (ISBN: 0198570007).

Checking Matrix Identities  
A. Nayak  
Encyclopedia of Algorithms. 4 pages.

A Separation between Divergence and Holevo Information for Ensembles  
Rahul Jain, Ashwin Nayak, and Yi Su.  
Technical Report arXiv:0712.3867. Submitted to TAMC 08, December, 2007. 13 pages.

Symmetrized Characterization of Noisy Quantum Processes  
J. Emerson, M. Silva, O. Moussa, C. Ryan, M. Laforest, J. Baugh, D. Cory, R. Laflamme  
Science 317, pp. 1893-1896 (2007).

Signatures of Incoherence in a Quantum Information Processor

M. K. Henry, A. Gorshkov, Y. Weinstein, P. Cappellaro, J. Emerson, Nicolas Boulant, Jonathan S. Hodges, Chandrasekhar Ramanathan, Timothy F. Havel, Rudy Martinez and David G. Cory  
Quantum Information Processing 6, 431-444 (2007).

Efficient Error Characterization in Quantum Information Processing  
B. Lévi, C. C. López, J. Emerson, and D. G. Cory  
Phys. Rev. A 75, 022314 (10 pages) (2007).

Symmetrisation Methods for Characterisation and Benchmarking of Quantum Processes  
J. Emerson  
Conference Proceedings for Theory Canada 4, Canadian Journal of Physics.

Scalable Experimental Protocol for Identification of Correctable Codes  
M. Silva, E. Magesan, D. Kribs, and J. Emerson  
Submitted to Phys. Rev. Lett. (2007).

Unconditional Security for Practical  
H. Inamori, N. Lütkenhaus, and D. Mayers  
Quantum Key Distribution; European Physical Journal D. Vol 41, p. 599 (2007)

On experimental procedures for entanglement verification  
S.J. van Enk, N. Lütkenhaus, H.J. Kimble  
Phys. Rev. A, Vol. 75, 052318 (2007)

Zero-Error Attacks and Detection Statistics in the Coherent One-Way Protocol for Quantum Cryptography  
C. Branciard, N. Gisin, N. Lütkenhaus, V. Scarani  
Quantum Information and Computation, Vol. 7, p. 639-664, 2007.

Sequential attacks against differential-phase-shift quantum key distribution with weak coherent states  
M. Curty, L.-L. Zhan, H.-K. Lo, N. Lütkenhaus  
Quantum Information and Computation, Vol 7, p 665-688, 2007.

Security of coherent state quantum cryptography in the presence of Gaussian noise  
M. Heid, N. Lütkenhaus  
Phys. Rev. A 76, 022313 (2007)

Optimal unambiguous state discrimination of two density matrices: A second class of exact solutions  
Ph. Raynal, N. Lütkenhaus  
Phys. Rev. A, Vol 76, 052322, 2007.

2008 Publications:

Optimizing the discrete time quantum walk using a  $SU(2)$  coin  
C. M. Chandrashekar, R. Srikanth, and Raymond Laflamme  
Phys. Rev. A 77, 032326 (2008)  
arXiv:0711.1882

Additivity and Distinguishability of Random Unitary Channels  
Bill Rosgen  
arXiv:0804.1936v1

Direct product theorems for classical communication complexity via subdistribution bounds  
Rahul Jain, Hartmut Klauck, Ashwin Nayak  
The 40th ACM Symposium on Theory of Computing (STOC) 2008

New bounds on classical and quantum one-way communication complexity  
Rahul Jain, Shengyu Zhang  
arXiv:0802.4101v1

Quantum Circuit Placement  
D. Maslov, S. M. Falconer, and M. Mosca  
IEEE Transactions on CAD 27(4):752-763, April 2008  
quant-ph/0703256

Quantum Circuit Simplification and Level Compaction  
D. Maslov, G. W. Dueck, D. M. Miller, and C. Negrevergne  
IEEE Transactions on CAD, 27(3):436-444, March 2008

Towards a world with quantum computers  
D. Bacon, D. Leung  
Comm. ACM, 50(9), 55 (2008)

The power of quantum systems on a line  
D. Aharonov, D. Gottesman, S. Irani, and J. Kempe  
Proc. 48th IEEE Symposium on the Foundations of Computer Science (FOCS), pp. 373-383 (2007).

Universal computation by quantum walk  
A. M. Childs  
arXiv:0806.1972.

Optimal quantum adversary lower bounds for ordered search  
A. M. Childs and T. Lee  
Proc. 35th International Colloquium on Automata, Languages and Programming, Lecture Notes in Computer Science 5125, pp. 869-880 (2008).

An exponential separation between the entanglement and communication capacities of a bipartite unitary interaction  
A. Harrow and D. Leung  
arXiv:0803.3066.

Coherent state exchange in multi-prover quantum interactive proof systems  
D. Leung, B. Toner, and J. Watrous  
arXiv: 0804.4118.

Quantum computational complexity  
J. Watrous  
arXiv: 0804.3401. To appear in Encyclopedia of Complexity and System Science, Springer, 2008.

Distinguishing quantum operations with few Kraus operators  
J. Watrous  
arXiv: 0710.0902. To appear in Quantum Information a

Number of Papers published in peer-reviewed journals: 78.00

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**(b) Papers published in non-peer-reviewed journals or in conference proceedings (N/A for none)**

Number of Papers published in non peer-reviewed journals: 0.00

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**(c) Presentations**

Number of Presentations: 0.00

Non Peer-Reviewed Conference Proceeding publications (other than abstracts):

Number of Non Peer-Reviewed Conference Proceeding publications (other than abstracts): 0

Peer-Reviewed Conference Proceeding publications (other than abstracts):

Number of Peer-Reviewed Conference Proceeding publications (other than abstracts): 0

(d) Manuscripts

Number of Manuscripts: 0.00

Number of Inventions:

Graduate Students

<u>NAME</u>	<u>PERCENT SUPPORTED</u>
Sevag Gharibian	0.08
William Rosgen	0.08
Ansis Rosmanis	0.08
Lana Sheridan	0.08
Sarvagya Upadhyay	0.08
Nathan Wiebe	0.06
David Yonge-Mallo	0.08
<b>FTE Equivalent:</b>	<b>0.54</b>
<b>Total Number:</b>	<b>7</b>

Names of Post Doctorates

<u>NAME</u>	<u>PERCENT SUPPORTED</u>
Rahul Jain	0.60
Dmitri Maslov	0.08
André Methot	0.08
Rolando Somma	0.00
Dmitry Gavinsky	0.65
Scott Aaronson	0.60
<b>FTE Equivalent:</b>	<b>2.01</b>
<b>Total Number:</b>	<b>6</b>

Names of Faculty Supported

<u>NAME</u>	<u>PERCENT SUPPORTED</u>	National Academy Member
Richard Cleve	0.00	No
Michele Mosca		No
Daniel Gottesman		No
Debbie Leung		No
Andrew Childs		No
Raymond Laflamme		No
John Watrous		No
Ashwin Nayak		No
Andris Ambainis		No
Peter Hoyer		No
Barry Sanders		No
David Kribs	0.25	No
Joseph Emerson		No
<b>FTE Equivalent:</b>	<b>0.25</b>	
<b>Total Number:</b>	<b>13</b>	

### Names of Under Graduate students supported

<u>NAME</u>	<u>PERCENT SUPPORTED</u>
<b>FTE Equivalent:</b>	
<b>Total Number:</b>	

### Student Metrics

This section only applies to graduating undergraduates supported by this agreement in this reporting period

The number of undergraduates funded by this agreement who graduated during this period: .....	0.00
The number of undergraduates funded by this agreement who graduated during this period with a degree in science, mathematics, engineering, or technology fields:.....	0.00
The number of undergraduates funded by your agreement who graduated during this period and will continue to pursue a graduate or Ph.D. degree in science, mathematics, engineering, or technology fields:.....	0.00
Number of graduating undergraduates who achieved a 3.5 GPA to 4.0 (4.0 max scale):.....	0.00
Number of graduating undergraduates funded by a DoD funded Center of Excellence grant for Education, Research and Engineering:.....	0.00
The number of undergraduates funded by your agreement who graduated during this period and intend to work for the Department of Defense .....	0.00
The number of undergraduates funded by your agreement who graduated during this period and will receive scholarships or fellowships for further studies in science, mathematics, engineering or technology fields: .....	0.00

### Names of Personnel receiving masters degrees

<u>NAME</u>	
Heath Gerhard	
William Rosgen	
Christoph Dankert	
Nathan Wiebe	
<b>Total Number:</b>	<b>4</b>

### Names of personnel receiving PHDs

NAME

Dmitry Gavinsky

Donny Cheung

Phillip Kaye

Carlos Perez-Delgado

Casey Myers

David Poulin

**Total Number:****6****Names of other research staff**NAMEPERCENT SUPPORTED

Wendy Reibel

0.00

No

Meghan Huras

No

Lorna Kropf

No

**FTE Equivalent:****0.00****Total Number:****3****Sub Contractors (DD882)****Inventions (DD882)**

## 1. Statement of the Problems Studied

The goal of the project is to discover new quantum algorithms; develop novel paradigms for constructing quantum algorithms; develop complexity-theoretic results that relate to quantum algorithms; and develop theoretical approaches for the implementation of quantum algorithms.

## 2. Summary of the Most Important Results

- We have contributed to the development of fast quantum algorithms for evaluating AND-OR trees (a.k.a. NAND trees), which are relevant in the context of evaluating optimal strategies in interactive settings (including various games). In particular, we showed how to obtain efficiency  $O(N^{1/2+\epsilon})$  for any  $\epsilon > 0$  in the discrete query setting, as well as how to generalize from balanced AND-OR trees to arbitrary AND-OR trees in the discrete query setting.
- We have extended the AND-OR results to algorithms for evaluating MIN-MAX trees.
- We have discovered an efficient quantum algorithm for searching among  $N$  items when the costs of querying the individual items are different. The algorithm runs in time  $O(\sqrt{T})$ , where  $T$  is the sum of the squares of the query times.
- In the area of lower bounds for algorithms, we have developed a new and more powerful variant of the adversary lower bound method, to handle negative weights.
- Finally, we have discovered a new efficient procedure for generating  $t$ -designs (which, roughly speaking, can be thought of as  $t^{\text{th}}$  order pseudorandom quantum states).
- We have shown that every quantum algorithm can be simulated by a continuous-time quantum walk of a simple form, and the methodology (using “widgets”) may lead to other applications in quantum algorithm design.
- We have clarified some notions about the “hitting times” for quantum walks (the time that it takes to get from one vertex to another), showing a quadratic speedup in the quantum case for a broad class of graphs.
- We have derived some improved quantum algorithms for simulating Hamiltonians that were previously known only for the sparse case.
- In the continuous-time query algorithmic paradigm (which is the paradigm where last year’s breakthrough result about NAND trees was first discovered), we have a general method for simulating a time  $T$  algorithm by a discrete quantum algorithm in time  $O(T \log T)$ . Previously, efficient simulations were known for some specific continuous-time algorithms; it was an open question whether this is always possible (a paper is forthcoming).
- Progress was made on an ongoing project concerning a quantum algorithm for the ferromagnetic Ising model (a paper is forthcoming).
- Regarding algorithms pertaining to quantum computing problems, we have further investigated the hardness of determining whether a bipartite quantum state (specified as a density matrix) is separable or entangled. This problem has long been known to be NP-hard—and thus likely hard even for quantum computers. However, the previous NP-hardness actually showed the problem is NP-hard in the case where exponential precision is required. This means that even entangled

states that are exponentially close to the separable region must be identified as entangled (even though their entanglement is exponentially small). We have shown that the problem remains NP-hard even if the precision is relaxed so as to be polynomial (as opposed to exponential). What this means is that it is unlikely that there is an efficient algorithm even for the problem of distinguishing separable states from those whose entanglement is significant (inverse polynomial in size).

- Finally, we have discovered a distributed computing problem that requires infinite entanglement to accomplish perfectly (and arbitrarily large entanglement to accomplish with arbitrary precision). This helps to explain why several complexity theoretic questions about multi-prover interactive proof systems have been very difficult to resolve: the underlying space of possible entangled states is not compact, and hence difficult to characterize in simple mathematical terms.

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